

DUE DATE: The homework problems from this handout are due **Monday, March 2nd**. There will also be a quiz in class on Monday, March 2nd.

**Section 9.1: Overview of the Technique** - The title here refers to solving linear equations  $y' = Ay$  where  $A$  is a square matrix of any size with constant components. We will review how to find the eigenvalues and eigenvectors of 2 by 2 matrices and discuss how these come up in the solution of  $y' = Ay$  when  $A$  is a 2 by 2 constant matrix.

**homework**: pg. 376-7, # 3, 8, 18, 21.

---

**Section 9.2: Planar Systems** - Restricting to  $y' = Ay$  for  $A$  a 2 by 2 constant matrix, the eigenvalues of  $A$  can be real and distinct, a complex conjugate pair, or real and repeated. We will discuss the general solution to  $y' = Ay$  in each case.

**homework**: pg. 389-91, # 16, 19, 25, 31, 37, 58a,b,c (you DO NOT need to produce the plot, just give the information about the eventual salt content and the reasons for your answer).

---

**Section 9.3: Phase Plane Portraits** - We already started to draw these in Chapter 8. Now, we add another key feature specifically for systems of the form  $y' = Ay$ : the general form of the phase portrait can be determined from the eigenvalues and eigenvectors of  $A$  (or equivalently from the trace and determinant of  $A$ ). Key concepts:

1. saddle point, separatrix
2. nodal sink, nodal source
3. spiral sink, spiral source
4. center
5. improper node

**homework**: pg. 401-2, # 10, 11, 14, 16, 21, 22. You do not need to turn in anything from a numerical solver, but you could use `pplane` in MATLAB to verify that your answers are correct. **BONUS**: Draw the complete phase plane portrait for

$$y' = \begin{pmatrix} -3 & -1 \\ 4 & 1 \end{pmatrix} y.$$