

HOMEWORK 5  
Due Oct 11

1. Exercises 9,10 page 56
2. Exercise 11 page 64
3. Suppose that  $A(t+T) = A(t)$  and that  $A(-t) = -A(t)$ . Let  $\Phi(t)$  be the principle fundamental matrix for  $x' = A(t)x$ . Show that  $\Phi(-t) = \Phi(t)$ . Use this to show that all solutions to  $x' = A(t)x$  are periodic.
4. Let  $A(t) = A(t+T)$  be a  $2 \times 2$  periodic matrix. The characteristic equation for the monodromy matrix can be written as

$$r^2 - ar + b.$$

The diagram below shows a triangle in the  $(a, b)$ -plane. Show that (a) All Floquet multipliers lie inside the unit circle if and only if  $(a, b)$  are in the triangle; (b) there exist  $T$ -periodic solutions along edge B; (c) there exist  $2T$ -periodic solutions along edge A; (d) what kinds of solutions exist along edge C? (Hint: the product of the multipliers is  $b$  and the sum is  $-a$ .)

